Tribhuwan University Institute of Science and Technology 2075(New Course)

Bachelor Level / second-semester / Science **Computer Science and Information Technology(MTH163)** (Mathematics II) Candidates are required to give their answers in their own words as far as practicable. The figures in the margin indicate full marks.

Group A

Attempt any three questions:(3 x 10 = 30)

1. When a system of linear equation is consistent and inconsistent? Give an example for each. Test the consistency and solve: x + y + z = 4, x + 2y + 2z = 2, 2x + 2y + z = 5.

2. What is the condition of a matrix to have an inverse? Find the inverse of the matrix

3. Define linearly independent set of vectors with an example. Show that the vectors (1, 4, 3), (0, 3, 1) and (3, -5, 4) are linearly independent. Do they form a basis? Justify.

4. Find the	least-square solution	n of Ax = b for
-------------	-----------------------	-----------------

Group B

Attempt any ten questions: (5 x 10 = 50)

 $\begin{pmatrix} 0 & 3 & -6 \\ 3 & -7 & 8 \\ 3 & -9 & 12 \end{pmatrix}.$

5. Change into reduce echelon form of the matrix $\sqrt{3}$ -9

6. Define linear transformation with an example. Is a transformation defined by T(x, y) = (3x + y, 5x + 7y, x + 3y) linear? Justify.

$$A = \begin{pmatrix} -1 & -2\\ 5 & 9 \end{pmatrix} \text{ and } \mathcal{B} = \begin{pmatrix} 9 & 2\\ k & -1 \end{pmatrix}$$

7. Let

What value (s) of k if any will make AB - BA?

8. Define determinant. Evaluate without expanding

$$H = \left\{ \begin{pmatrix} s \\ t \\ 0 \end{pmatrix} : s, t \in \mathbb{R} \right\}.$$

9. Define subspace of a vector space. Let

Show that H is a subspace of:

(c) - page 1of 2 Find more question papers at collegenote.pythonanywhere.com

$A = \begin{pmatrix} 1 & -2 & -1 \\ -1 & 5 & 6 \\ 5 & -4 & 5 \end{pmatrix}$

Time: 3 hours

 $A = \begin{pmatrix} 1 & 3 & 5 \\ 1 & 1 & 0 \\ 1 & 1 & 2 \\ 1 & 3 & 3 \end{pmatrix} \text{ and } b = \begin{pmatrix} 3 \\ 5 \\ 7 \\ 3 \end{pmatrix}.$

(5 - 4 5) 4, 3), (0, 3, 1) and (3, -5, 4

Pass marks: 32

in exists.

Full marks: 80

$$A = \begin{pmatrix} -3 & 6 & -1 & 1 & -7 \\ 1 & -2 & 2 & 3 & -1 \\ 2 & -4 & 5 & 8 & -4 \end{pmatrix}$$

10. Find the dimension of the null space and column space of

$$\begin{pmatrix} 6 & 3 & -8 \\ 0 & -2 & 0 \\ 1 & 0 & -3 \end{pmatrix}.$$

11. Find the eigenvalues of the matrix

$$\begin{pmatrix} 2 & 5 \\ 6 & -7 \end{pmatrix}$$

12. Find LU factorization of the matrix $\begin{pmatrix} 0 & -7 \end{pmatrix}$

13. Define group. Show that the set of all integers Z forms group under addition operation.

14. Define ring with an example. Compute the product in the given ring (-3, 5) (2, -4) in $Z_4 \times Z_{11}$.

15. State and prove the Pythagorean theorem of two vectors and verify this for u = (1, -1) and v = (1, 1).