

**TRIBHUVAN UNIVERSITY**  
**Institute of Science and Technology**  
2072

Bachelor Level/ Second Year/ Third Semester/ Science  
**Computer Science and Information Technology**  
(CSc.204) (Numerical Method)

Full Marks: 60  
Pass Marks: 24  
Time: 3 hours

*Candidates are required to give their answers in their own words as far as practicable. The figures in the margin indicate full marks.*

**Attempt all questions:**

1. What are the sources of errors? Discuss various types of errors. Find the roots of the equation  $x^2 + 5.6x - 10 = 0$  by trial and error method up to 4 significant digits. (1+3+4)
2. Describe Newton's method and its convergence. Find the root of equation  $f(x) = ex - 4x^2 = 0$  using Newton method up to 5 decimal places. (4+4)
3. What do you mean by interpolation and approximation? Use Lagrange interpolation to estimate the value of  $f(0.6)$  from the following table of values. (2+6)

x	0.4	0.5	0.7	0.8
f(x)	-0.916	-0.693	-0.357	-0.223

4. Using Newton's divided difference interpolating polynomial estimate the value of  $f(x)$  at  $x = 2.25$  for the function defined as

x	0.5	0.2	1.4	2.2	3.0
f(x)	-10.25	-3.768	5.976	28.972	79.0

5. Write algorithm for Gauss- Seidel method for solving the system of linear equations. Also solve the following system of linear equations using that method. (4+4)

$$1 \quad 0x_1 + x_2 + x_3 = 12$$

$$x + 10x_2 + x_3 = 10$$

$$-2x_2 + 10x_3 = 9$$

6. What do you understand by the partial differential equation? Illustrate it with practical example and derive difference equation. (8)

**OR**

Find the solution of following differential equations using Taylor series method.

$$y = (x^3 + xy^2)e^{(-x)}, y(0) = 1, \text{ to find } y \text{ at } x = 0.1, 0.2, 0.3.$$

7. Write an algorithm and program for computer to obtain the solution of differential equation using Runge-Kutta Method. (5+7)

Candidates are required to give their answers in their own words as far as practicable. The figures in the margin indicate full marks.

**Attempt all questions:**

8. What are the sources of errors? Discuss various types of errors. Find the roots of the equation  $x^2 + 5.6x - 10 = 0$  by trial and error method up to 4 significant digits. (1+3+4)
9. Describe Newton's method and its convergence. Find the root of equation  $f(x) = ex - 4x^2 = 0$  using Newton method up to 5 decimal places. (4+4)
10. What do you mean by interpolation and approximation? Use Lagrange interpolation to estimate the value of  $f(0.6)$  from the following table of values. (2+6)

x	0.4	0.5	0.7	0.8
f(x)	-0.916	-0.693	-0.357	-0.223

11. Using Newton's divided difference interpolating polynomial estimate the value of  $f(x)$  at  $x = 2.25$  for the function defined as

x	0.5	0.2	1.4	2.2	3.0
f(x)	-10.25	-3.768	5.976	28.972	79.0

12. Write algorithm for Gauss- Seidel method for solving the system of linear equations. Also solve the following system of linear equations using that method. (4+4)

$$10x_1 + x_2 + x_3 = 12$$

$$x_1 + 10x_2 + x_3 = 10$$

$$-2x_2 + 10x_3 = 9$$

13. What do you understand by the partial differential equation? Illustrate it with practical example and derive difference equation. (8)

**OR**

Find the solution of following differential equations using Taylor series method.

$$y = (x^3 + xy^2)e^{-x}, y(0) = 1, \text{ to find } y \text{ at } x = 0.1, 0.2, 0.3.$$

14. Write an algorithm and program for computer to obtain the solution of differential equation using Runge-Kutta Method. (5+7)